

## Heavy metal AND

### Metal flux

$$\frac{dmet_1}{dt} = \frac{K_{cat\ met1\ in}\ MntH\ met_{1\ out}}{k_m\ met_{1\ in} + met_{1\ out}} - \frac{k_{cat\ met1\ out}\ CadA\ met_1}{k_m\ met_{1\ out} + met_1}$$

$$\frac{dmet_2}{dt} = \frac{K_{cat\ met2\ in}\ MntH\ met_{2\ out}}{k_m\ met_{2\ in} + met_{2\ out}} - \frac{k_{cat\ met2\ out}\ ArsB\ met_2}{k_m\ met_{2\ out} + met_2}$$

### ArsR and CzrA production

$$\frac{dRna_{ArsR}}{dt} = \beta_{transc\ ArsR} \left( \frac{1}{1 + \left( \frac{1}{K_a\ ArsR} \right)^n} \right) - \alpha_{Rna\ ArsR} Rna_{ArsR}$$

$$\frac{dArsR}{dt} = \beta_{transl\ ArsR} Rna_{ArsR} - \alpha_{ArsR} ArsR$$

$$ArsR^* = \frac{ArsR}{1 + \left( \frac{arabinose}{K_a\ arabinose} \right)^n}$$

$$\frac{dRna_{CzrA}}{dt} = \frac{V_{max\ CzrA}\ Met_1}{K_m\ CzrA + Met_1} - \alpha_{Rna\ CzrA} Rna_{CzrA}$$

$$\frac{dCzrA}{dt} = \beta_{transl\ CzrA} (Rna_{CzrA}) - \alpha_{CzrA} CzrA$$

$$1\ CzrA^* = \frac{CzrA}{1 + \left( \frac{met_1}{K_a\ met_1} \right)^n}$$

### CadA y ArsB transporter

$$\frac{dRna_{CadA}}{dt} = \beta_{transc\ CadA} \left( \frac{1}{1 + \left( \frac{1}{K_{CzrA}} \right)^n} \right) - \alpha_{Rna\ CadA} Rna_{CadA}$$

$$\frac{dCadA}{dt} = \beta_{transl\ CadA} Rna_{CadA} - \alpha_{CadA} CadA$$

$$\frac{dRna_{ArsB}}{dt} = \beta_{transc\ ArsB} \left( \frac{1}{1 + \left( \frac{1}{K_a\ ArsR} \right)^n} \right) - \alpha_{Rna\ ArsB} Rna_{ArsB}$$

$$\frac{dArsB}{dt} = \beta_{transl\ ArsB} Rna_{ArsB} - \alpha_{ArsB} ArsB$$

### AND output P4/LasR

$$\frac{dRna_{P4}}{dt} = \beta_{transc\ P4} \left( \frac{1}{1 + \left( \frac{1}{K_a\ CzrA} \right)^n} \right) \left( \frac{1}{1 + \left( \frac{1}{K_a\ ArsR} \right)^n} \right) - \alpha_{Rna\ P4} Rna_{P4}$$

$$\frac{dP4}{dt} = \beta_{transl\ P4} Rna_{P4} - \alpha_{P4} P4$$

$$\frac{dRna_{LasR}}{dt} = \beta_{transc\ LasR} \left( \frac{1}{1 + \left( \frac{1}{K_a\ CzrA} \right)^n} \right) \left( \frac{1}{1 + \left( \frac{1}{K_a\ ArsR} \right)^n} \right) - \alpha_{Rna\ LasR} Rna_{LasR}$$

$$\frac{dLasR}{dt} = \beta_{transl\ LasR} Rna_{LasR} - \alpha_{LasR} LasR$$

Sweet AND

Sugar uptake

$$\frac{d \text{arabinose}}{dt} = \frac{\beta_{\text{upt arabinose}} \text{AraE arabinose}}{K_m \text{AraE} + \text{AraE}} - \frac{K_{\text{cat AraA}} \text{AraA arabinose}}{\text{arabinose} + K_m \text{AraA}}$$

$$\frac{d \text{xylose}}{dt} = \frac{\beta_{\text{upt arabinose}} \text{AraE arabinose} /}{K_m \text{AraE} + \text{AraE}} - \frac{K_{\text{cat XylA}} \text{XylA xylose}}{(\text{xylose} + K_m \text{XylA})}$$

AraR and XylR TF production

$$\frac{d \text{Rna}_{\text{AraR}}}{dt} = \beta_{\text{transc AraR}} \left( \frac{1}{1 + \left( \frac{\text{AraR}^*}{K_{\text{AraR}}} \right)^n} \right) - \alpha_{\text{Rna AraR}} \text{Rna}_{\text{AraR}}$$

$$\frac{d \text{AraR}}{dt} = \beta_{\text{transl AraR}} \text{Rna}_{\text{AraR}} - \alpha_{\text{AraR}} \text{AraR}$$

$$\text{AraR}^* = \frac{\text{AraR}}{1 + \left( \frac{\text{arabinose}}{K_{\text{arabinose}}} \right)^n}$$

$$\frac{d \text{Rna}_{\text{XylR}}}{dt} = \beta_{\text{transc XylR}} (1 + q_{\text{XylR}} \text{xylose}) + \beta_{\text{transc XylR Pveg}} - \alpha_{\text{Rna XylR}} \text{Rna}_{\text{XylR}}$$

$$\frac{d \text{XylR}}{dt} = \beta_{\text{transl XylR}} (\text{Rna}_{\text{XylR}}) - \alpha_{\text{XylR}} \text{XylR}$$

$$\text{XylR}^* = \frac{\text{XylR}}{1 + \left( \frac{\text{xylose}}{K_{\text{xylose}}} \right)^n}$$

Transport and metabolism proteins

$$\frac{d \text{Rna}_{\text{AraA}}}{dt} = \beta_{\text{transc AraA}} \frac{1}{\left( 1 + \left( \frac{\text{AraR}^*}{K_a \text{AraR}} \right)^n \right)} - \alpha_{\text{Rna AraA}} \text{Rna}_{\text{AraA}}$$

$$\frac{d \text{Rna}_{\text{AraE}}}{dt} = \beta_{\text{transc AraE}} \left( \frac{1}{1 + \left( \frac{\text{AraR}^*}{K_a \text{AraR}} \right)^n} \right) - \alpha_{\text{Rna AraE}} \text{Rna}_{\text{AraE}}$$

$$\frac{d \text{Rna}_{\text{XylA}}}{dt} = \beta_{\text{transc XylA}} \frac{1}{\left( 1 + \left( \frac{\text{XylR}^*}{K_a \text{XylR}} \right)^n \right)} - \alpha_{\text{Rna XylA}} \text{Rna}_{\text{XylA}}$$

$$\frac{d \text{XylA}}{dt} = \beta_{\text{transl XylA}} \text{Rna}_{\text{XylA}} - \alpha_{\text{XylA}} \text{XylA}$$

$$\frac{d \text{Rna}_{\text{AraC}}}{dt} = \beta_{\text{transc AraC}} - \alpha_{\text{Rna AraC}} \text{Rna}_{\text{AraC}}$$

$$\frac{d \text{AraC}}{dt} = \beta_{\text{transl AraC}} \text{Rna}_{\text{AraC}} - \alpha_{\text{AraC}} \text{AraC}$$

LasR/P4 expression

$$\frac{d \text{Rna}_{\text{LasR}}}{dt} = \beta_{\text{transc LasR}} \frac{\text{arabinose}^n}{K_a^n \text{arabinose} + \text{arabinose}^n} \left( \frac{1}{1 + \left( \frac{\text{XylR}^*}{K_a \text{XylR}} \right)^n} \right) - \alpha_{\text{Rna LasR}} \text{Rna}_{\text{LasR}}$$

$$\frac{dLasR}{dt} = \beta_{transl LasR} Rna_{LasR} - \alpha_{LasR} LasR$$

$$\frac{dRna_{P4}}{dt} = \beta_{transc P4} \left( \frac{1}{1 + \left( \frac{AraC^*}{K_a AraC} \right)^n} \right) \left( \frac{1}{1 + \left( \frac{XylR^*}{K_{XylR}} \right)^n} \right) - \alpha_{Rna P4} Rna_{P4}$$

$$\frac{dP4}{dt} = \beta_{transl P4} Rna_{P4} - \alpha_{P4} P4$$

OR

$$\frac{dRna_{GusA}}{dt} = \beta_{GusA P4} \left( \frac{(1 + \left( \frac{P4}{K_{P4}} \right)^n \omega)}{1 + \left( \frac{P4}{K_{P4}} \right)^n} \right) + \beta_{GusA LasR} \left( \frac{(1 + \left( \frac{LasR}{K_{LasR}} \right)^n \varphi)}{1 + \left( \frac{LasR}{K_{LasR}} \right)^n} \right) - \alpha_{Rna GusA} Rna_{GusA}$$

$$\frac{dGusA}{dt} = \beta_{transl GusA} Rna_{GusA} - \alpha_{GusA} GusA$$